

Week 15 - Spring 2014 Solutions

Exercise 1.1

a) We can use expression (1) to solve for equilibrium level of

$$Y^* = 4(200 + 200 + 300 - 100) - 3(200) = 1800$$

Then,

$$C = 200 + 0.75(1800 - 200) = 1400$$

$$S_p = -200 + (1 - 0.75)(1800 - 200) = 200$$

We can also check if the model is well defined by computing: $I - S_g + S_p = KI$. Then,

$$200 - (200 - 100) = 100$$

b) We have two different goals: achieve full employment level of output $Y_{fe} = 2000$ ($\Delta Y = (2000 - 1800) = 200$) and equilibrate government budget ($\Delta S_g = 100$)

Therefore, we need to solve the following system of two equations in two unknowns:

$$200 = 4\Delta G - 3\Delta T$$

$$100 = \Delta T - \Delta G$$

Then $\Delta T = 600$ and $\Delta G = 500$. So the new levels of G and T are 800 each.

Exercise 1.2

The new multiplier is:

$$Y = \frac{1}{1 - c(1 - t) - i + m} [C_0 - c(T - TR) + I_0 + G + X - M_0]$$

Notice that our multiplier is more complex now because we have more terms that depend on income.

a) If government increases G by \$100, the equilibrium GDP will increase \$200 since the expenditure multiplier is 2.

b) Initial GDP is $Y = 2 * (200 - 0.8 * 100 + 300 + 600 + 480 - 250) = 2 * 1250 = 2500$. When $m = 0.3$, the multiplier becomes 1.79, so GDP is $Y = 1.79 * 1250 = 2232.15$

c) The new policy implies $TR = 0.2M = 0.2(250 + 0.3Y) = 50 + 0.06Y$. Also notice that the multiplier becomes $\frac{1}{1 - 0.8(1 - 0.2 + 0.06) - 0.1 + 0.3} = 1.9531$ and the Autonomous part is $1250 + 0.8(50) = 1290$

Therefore, $Y = 1.9531 * 1290 = 2519.5$

Exercise 2.1

a- Since they only have to hold \$100 in reserves, instead of \$200, banks now lend out \$100 of their reserves. Whoever borrows the \$100 will deposit in a bank, which will

lend out $\$100 \cdot (1-.1) = \90 . Whoever borrows the \$90 will put it in a bank, which will lend out \$81, and so on. Overall, deposits increase by $\$100/.1 = \1000 .

- b- Again, banks lend out \$100 of their reserves. Whoever borrows the \$100 will keep \$50 in cash and deposit \$50 in a bank. The bank will lend out $\$50 \cdot .9 = \45 . Whoever borrows the \$45 will keep \$22.5 in cash and deposit \$22.5 in a bank, and so on.

Exercise 2.2

OM purchase of \$100 million by the Fed increases banks' reserves as the Fed credits their accounts with additional reserves (i.e. monetary base goes up by \$100). Since those are extra reserves beyond the minimum requirements, banks lend out \$100 million. Same analysis as before....

Exercise 2.3

Federal Reserve		Banks	
Assets	Liabilities	Assets	Liabilities
Treasury bills -100	Monetary base -100	Treasury bills 100	Deposits -500
		Reserves -100	
		Loans -500	